MATH6015: Test 2 Sample Winter 2016

This is the same as the sample in the notes except that questions four and six have been replaced by a single question on area.

Answer all questions. Marks may be lost if necessary work is not clearly shown.

1. Find
$$\int \left(4t^4 - \frac{3}{t} - 5e^{-0.1t} - 1\right) dt$$
.

[5 Marks]

2. Evaluate
$$\int_0^4 \frac{16}{x^2 + 16} dx$$

[5 Marks]

3. Evaluate
$$\int_0^1 x(0.01x - x^2) dx$$
.

[5 Marks]

4. Find
$$\int 9x^2(x^3+2)^{10} dx$$
.

[5 Marks]

5. Find
$$\int \sec^2(e^x) 2e^x dx$$
.

[5 Marks]

6. Find
$$\int \frac{(\ln y)^2}{y} dy$$
.

[5 Marks]

7. (a) Find the intersection of the curves
$$y = x$$
 and $y = 4x - x^2$.

[3 Marks]

(b) Hence, on a single diagram, draw a rough sketch of the curves
$$y = x$$
 and $y = 4x - x^2$.

[1 Mark]

(c) Hence, find the area enclosed by the two curves.

[6 Marks]